

PULSED INDUCTIVE THRUSTER (PIT); MODELING AND VALIDATION USING THE MACH2 CODE

Pavlos G. Mikellides[^]

Arizona State University
Tempe, AZ 85287-6106

ABSTRACT

Numerical modeling of the Pulsed Inductive Thruster exercising the magnetohydrodynamics code, MACH2 aims to provide bilateral validation of the thruster's measured performance and the code's capability of capturing the pertinent physical processes. Computed impulse values for helium and argon propellants demonstrate excellent correlation to the experimental data for a range of energy levels and propellant-mass values. The effects of the vacuum tank wall and mass-injection scheme were investigated to show trivial changes in the overall performance.

INTRODUCTION

The Pulsed Inductive Thruster (PIT) is a unique propulsion system due to a combination of its distinctive physical operation, demonstrated performance and potential advantages over all other electric rockets.¹ A spiral induction coil is powered by a series of capacitors in Marx-loop configurations and produces a strong azimuthal electric field once the pulsed current is passed through. The field breaks down the injected propellant over the surface of the flat coil and the associated radial magnetic field induces an azimuthal current within a thin gas layer. (Fig. 1) This current interacts with the magnetic field to produce an axially-directed electromagnetic force. Such inductive acceleration circumvents the need for electrodes and the erosion-related lifetime limitations that plague traditional electromagnetic thrusters. The PIT can operate with any propellant, however single-shot operation demonstrated optimum performance with polyatomic-molecule fuel. Specifically, the PIT-MkV operating with ammonia at 4.6kJ demonstrated nearly-constant efficiencies exceeding 50% for a wide range of specific-impulse values; $4000s < I_{sp} < 8000s$. Its propensity to work best with such fuels renders the thruster ideal for water-propellant operation and associated missions such as In-Situ Propellant Utilization (ISRU) where refueling can be realized by appropriate water-rich cometary rendezvous or by capitalizing on Europa's oceans for deeper space assignments. Its pulsed operation can provide elevated maneuverability -- the aforementioned operation produced an impulse range of $0.05N\cdot s < I\text{-bit} < 0.12 N\cdot s$ -- which in conjunction to its water-propellant affinity establishes the concept very attractive for Orbital Express Architectures during which satellites can refuel and upgrade electronics by docking to on-orbit modules.

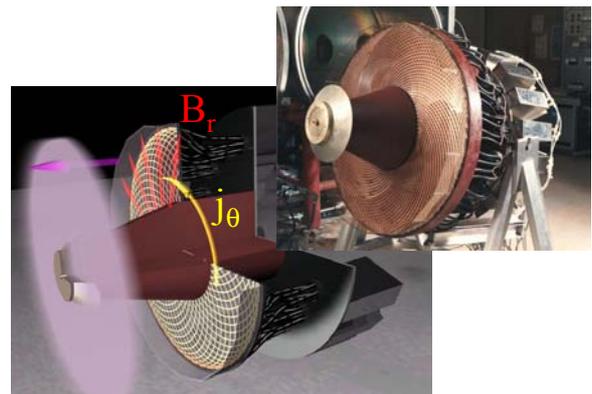


Figure 1. The Pulsed Inductive Thruster (PIT) (Courtesy TRW) and a schematic of the relative acceleration process due to the dominant interaction of the applied radial field and the induced azimuthal current.

In order to provide added confidence in the PIT's demonstrated capabilities the magnetohydrodynamics (MHD) code, MACH2 is employed to model its operation and offer preliminary validation by comparisons with experiments. Specifically, the paper aims to validate the code's capabilities in capturing the pertinent physics by comparing experimental results to the numerical findings.

[^] Assistant Professor, Department of Mechanical and Aerospace Engineering, P.O. Box 876106, Phone: (480) 727-6215, E-mail: Pavlos.Mikellides@asu.edu, Member AIAA.

NUMERICAL MODEL

MACH2 is a time-dependent, two-dimensional, axisymmetric, multi-material code that can be applied to problems of complex geometries due to its multi-block structure.² The computational mesh can move in an Arbitrary-Lagrangian-Eulerian (ALE) fashion allowing applicability to both diffusive- and dispersive-dominated problems as well as code validation. The mesh can be refined via a variety of adaptive schemes to capture regions of varying characteristic scale. The set of the single-fluid, MHD equations is time-advanced with finite-volume spacial differencing, and the boundary conditions are applied via the ghost-cell technique so that no special conditional statement is necessary at the boundaries.

The mass continuity and momentum equations assume a compressible, viscous fluid with the latter including both real and artificial viscosity effects. The stress-deviator can be chosen to evolve under elastic stress for strength of material calculations³ or modeled as a Newtonian fluid to upgrade the code to a Navier-Stokes solver.¹¹ The code includes two ablation models that allow mass addition due to solid evaporation and have been successfully employed to model ablation-fed pulsed plasma thrusters.⁴ The electrons, ions and radiation field are in thermal non-equilibrium, so MACH2 solves three energy equations. These include thermal conduction with anisotropic transport⁵ and three different models for radiation cooling.^{21,6} Evolution of the magnetic field is prescribed by the induction equation that includes resistive diffusion, the Hall effect and the thermal source for magnetic fields. Various models for the plasma resistivity are available. They comprise classical anisotropic resistivity,²⁶ several anomalous resistivity models and contributions from electron-neutral collisions applicable to weakly ionized gases.²¹ In many engineering applications the source of magnetic flux is applied currents produced from externally-applied voltage differentials. For this, the code includes a variety of circuit models such as LRC, Pulse-Forming-Networks, sine-waveforms and several others. Other additional physical models include laser-pulse energy deposition and a detonation package. The set of the MHD equations is completed by an equation of state that can be either analytic or tabular. The latter is provided by the SESAME library that includes semi-empirical models for the thermodynamic properties, transport coefficients, (including opacities) and average ionization state under local thermodynamic equilibrium. These models have been constructed and are being maintained by the T-1 and T-4 groups at Los Alamos National Laboratory.⁷

The level of sophistication and capability of the MACH2 code has been instrumental in providing invaluable insights to a variety of plasma problems. Some of these include plasma opening switches,⁸ inertial-confinement fusion and alternative concepts,⁹ compact toroid formation and acceleration schemes,¹⁰ gas and solid density z-pinch implosion physics,¹¹ laser-target interactions,¹² high-power plasma source design,¹³ magnetic nozzles¹⁴ and a variety of plasma thrusters.^{11,16} Its diverse success establishes the code as a primary numerical tool toward the understanding of the intricate physical processes and feasibility issues of the proposed propulsion concept.

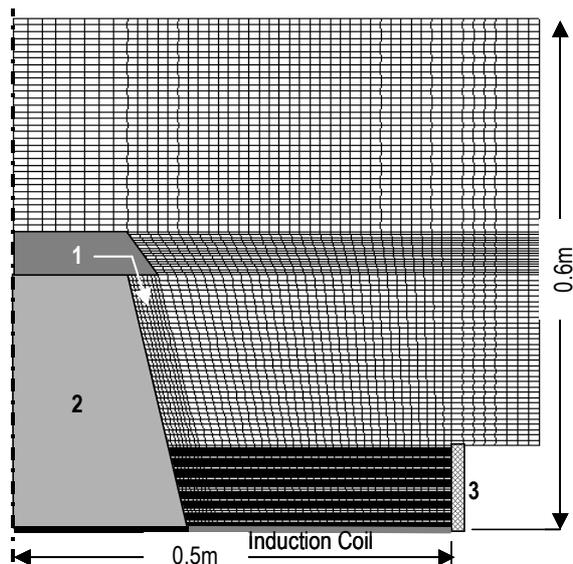


Figure 2. Schematic of the half-plane thruster with the computational grid utilized, (to scale). 1: Nozzle with pulsed mass-valve, 2: Conical pylon, 3: Confining cuff (lexan).

PIT PHYSICAL MODELING

A substantial body of experimental data is available for the Pulsed Inductive Thruster (PIT) comprising a diverse range of propellants, energy levels and propellant mass values.^{1,15} The power supply consists of a series of 18 capacitors in Marx-loop pairs that are charged in parallel. This results in an effective discharge voltage that is double that of the each capacitor's charge voltage which in turn provides the necessary high electric fields for breakdown. In particular, the configuration results in an effective capacitance and voltage that relate to the single capacitance and charge voltage through the total energy available:

$$E_o = \frac{1}{2}(\text{\#of capacitors})CV_o^2 = \frac{1}{2}C_{\text{eff}}V_{\text{eff}}^2 \quad (1)$$

where $V_o = 1/2V_{\text{eff}}$. For the polyatomic propellant experiments

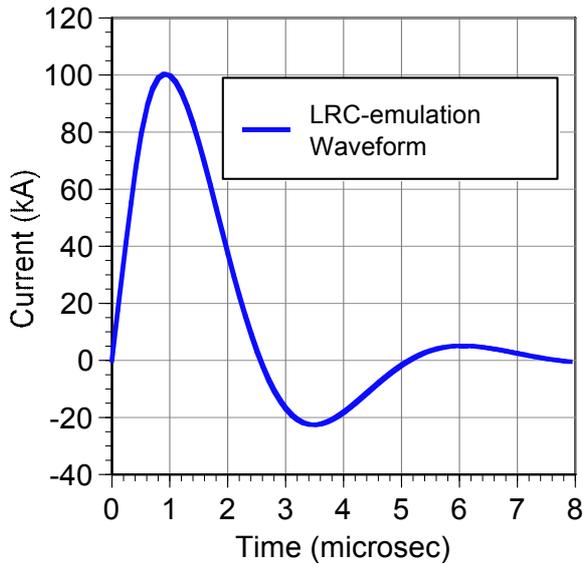


Figure 3. Calculated Current waveform used to emulate the PIT's circuitry, $V_{\text{eff}}=28\text{kV}$.

the effective capacitance was $9\mu\text{F}$ while the earlier efforts with monatomic propellants utilized smaller capacitors with effective capacitance of $4.5\mu\text{F}$. The resulting oscillatory current waveform provided pulse duration of the order of $15\mu\text{sec}$ with peak currents exceeding 100kA for a range of charge voltage of $10\text{kV} < V_0 < 16\text{kV}$ and propellant mass of $1.5\text{mg} < m < 10\text{mg}$. Mass is introduced through a nozzle (Fig. 2) by a fast opening gas valve. For optimal distribution of the injected gas the mass-pulse is short enough such that it ceases as the leading edge reaches the confining lexan. The PIT's performance data exhibited approximately-constant-efficiency trends for a wide range of specific impulse values ($500\text{s} < I_{\text{sp}} < 9000\text{s}$) providing impulses exceeding $0.1\text{ N}\cdot\text{s}$. Monatomic propellants demonstrated efficiencies on the order of 20% while polyatomic propellants with the higher-capacitance bank dramatically improved exhibiting maximum efficiencies above 50% with ammonia.

The MACH2 simulations utilized the helium and argon data for comparisons as the SESAME tables provided a complete real equation of state that includes a degree of ionization semi-empirical model. The physical model included thermal non-equilibrium of a single-viscous fluid with classical transport. Boundary conditions modeled thermal and magnetic field insulators with no-slip. The computational grid (Fig. 2) extended well downstream of the thruster's exhaust region to comprehensively capture the acceleration process and assure no influence of the outlet boundary conditions that model variables at zero gradient. Grid resolution was maximized in the vicinity of the coil to assure capture of the fast-rising field's diffusion and associated gradient. In particular, the significant acceleration process occurs during the rise-time, $t_r \sim 0.9\mu\text{sec}$, which implies a characteristic diffusion depth of about 1.78cm for a 2eV plasma, ($\delta \sim [\eta t_r]^{1/2}$, where $\eta \sim 1000/T_e^{3/2}\text{ m}^2/\text{s}$ is the electrical diffusivity with T_e in eV). The axial grid-cell dimension, $\Delta z = 1.56\text{mm}$ assures accurate capture of the field's gradient with more than 10 cells resolving the diffusion depth.

Initial conditions assigned uniform density in the vicinity of the coil (the confined region shown by the highest-resolution grid in Figure 2) - to at best resemble the evolved gas injected from the valve - and uniform room temperature. The significance of non-uniformities present due to the injection scheme is addressed later. This implies that ionization of the gas which occurs after the breakdown is calculated by the MACH2 ionization model consistently with the evolution of the rest of the pertinent variables. Emulation of the current waveform used the LRC circuit model. Specifically, a circuit model had been developed¹ to calculate the PIT's current waveform with significant accuracy.¹⁵ For the MACH2 simulation the LRC external parameters were adjusted to as-best match the important features of the aforementioned model. The comparison is shown in Table 1 and the LRC current waveform used to simulate helium operation is depicted in Fig 3.

	<u>PIT</u>	<u>MACH2-LRC</u>
$V_{\text{eff}}, E:$	28kV, 1764J	28kV, 1764J
$J_{\text{max}}, t_{\text{rise}}:$	100kA, 0.75 μs	100kA, 0.9 μs
First zero, $t_0:$	3 μs	2.7 μs
$J_{\text{min}}:$	-40kA	-22.6kA

Table 1. Comparison of relevant characteristics of the PIT and LRC emulated waveforms.

It should be emphasized that the PIT circuit model included a semi-empirical statement of the plasma's inductance axial variation along with the plasma's resistance influence. The MACH2 LRC model even though it does include the influence of the latter, it does not presently include the inductance variation.

Thrust calculation was performed at the outlet boundaries as the integral of the dynamic pressure and integrated to provide the impulse. This implied that even though the effective pulse duration was about $8\mu\text{s}$ computational

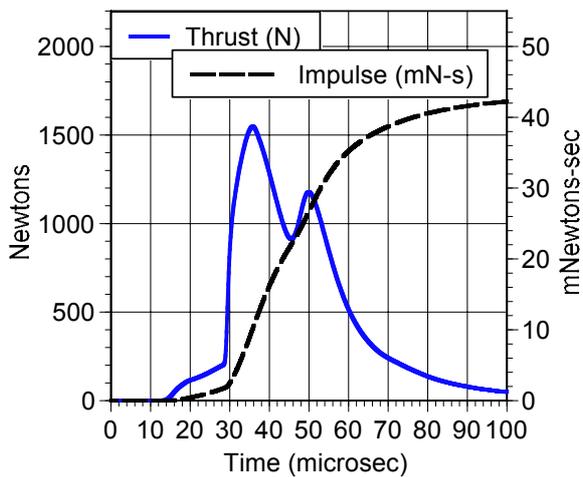


Figure 4. Calculated thrust histogram and associated impulse evolution, $V_{\text{eff}}=28\text{kV}$, $m=3\text{mg}$.

thrust values would indicate better coupling and thus increased exhaust velocities for the same propellant mass and energy level. In turn, the aforementioned observations imply a substantially effective coupling of plasma and magnetic flux that allows induction of significant currents and consequently electromagnetic force. Such behavior is quite encouraging as it suggests that MACH2 captures the relevant coupling mechanisms as expected from such concept.

COMPARISONS WITH EXPERIMENT

Computations using the MACH2 code were performed for the range of available charge voltage and propellant mass. Specifically, experiments addressed a range of energy levels between 900J and 1764J with propellant mass variation from 0.75mg to 9.2mg. For each pair, data for the impulse were provided which in turn produced the range of specific impulse and efficiency values. MACH2 was invoked to compute all the different arrangements for a full range comparison of Impulse vs specific energy illustrated in Figures 5-8. The computed impulse correlates very well with the experimental values. MACH2 computed impulse values for the 900J case exhibit an overestimation of about 10% when compared to the single experimental point. This discrepancy is partially attributed to an experimentally observed critical-mass value below which incomplete breakdown was observed along with the consequent reduction in impulse. Even though the code can not address breakdown physics, this implicit incomplete coupling of plasma and magnetic flux is partially reflected by the computations as indeed efficiency is decreasing with decreasing propellant mass value. However, the magnitude of this reduction is not fully captured by the code's physical models and thus the overestimation. It is of interest to note though, that MACH2's partial capture of this critical-mass trend is indicative of additional influencing processes other than breakdown behavior.

Even though the comparisons with experimental data are extremely encouraging certain simplifications and deficiencies of the code at its present state may be offsetting so as to result in the computed accuracy. In particular, three issues arise. Experimental data were obtained in a restricted vacuum tank of 1.2 m in diameter (the thruster's diameter is 1 m) while the simulations implemented a free (outlet) boundary condition for the exhausting plasma. (See Figure 2, the right outermost boundary of the computational region.) The simulations assumed uniform initial conditions over the surface of the induction coil - which may tend to overestimate the calculated impulse values as uniform flux coupling is encouraged - and the lack of the LRC circuit model reaction to the plasma dynamics resulted in a current waveform that underestimates the second current peak by almost half. The latter two issues may be actually offsetting each other as any underestimation of the acceleration from the second current peak may be equalized by the aforementioned inaccuracy due to uniform initial conditions. For this the first two issues were addressed.

times needed to be in excess of $100\mu\text{s}$ so as to capture exhaust of all the propellant through the downstream boundaries. The thrust histogram for the representative case of $V_o = 14\text{kV}$ and $m=3\text{mg}$ is shown in Figure 4 along with the evolution of the impulse. The sharp rise of the thrust value at about $30\mu\text{sec}$ suggests exhaust of a compact plasma consistent with a slug-acceleration notion.

This was confirmed by inspection of the two-dimensional density distribution as calculated by the code; they depicted a fairly sharp mass outline that included the majority of the propellant. The second peak in the evolution proposes additional acceleration of part of the remaining mass by the second peak at minimum current. The reduced gradient especially after the peak suggests a more dispersed plasma that takes longer to pass through the exhausting boundary. The width of the thrust pulse also indicates the degree of effective coupling and of course the eventual exhaust speed.

In other words, a narrower histogram with higher peak

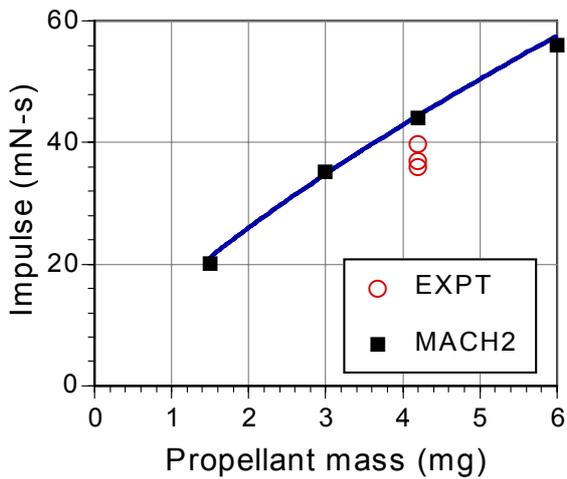


Figure 5. MACH2 impulse comparison with experimental data for helium and 900J.

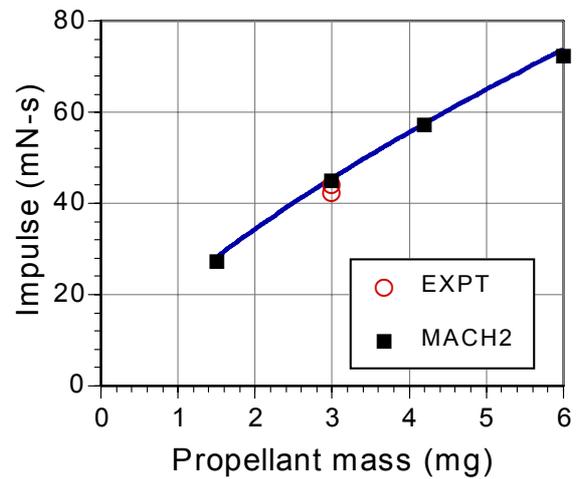


Figure 7. MACH2 impulse comparisons with experimental data for helium and 1764J.

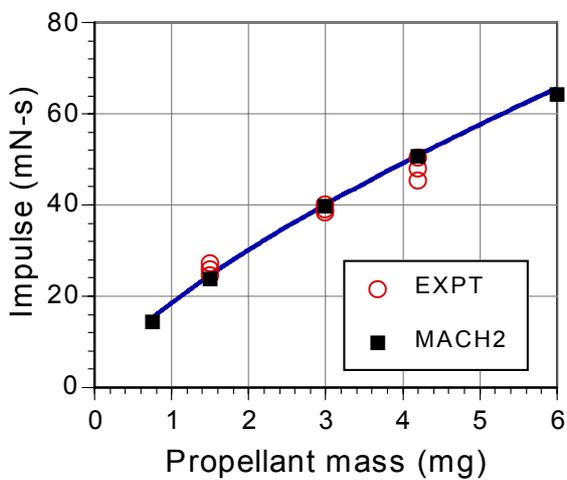


Figure 6. MACH2 impulse comparison with experimental data for helium and 1296J.

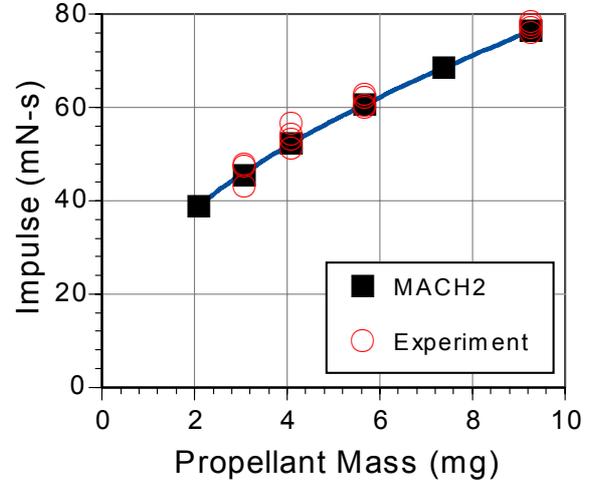


Figure 8. MACH2 impulse comparisons with experimental data for argon and 1764J.

A new set of simulations was contrived that would emulate the vacuum tank's walls at 0.1m away from the confining lexan. This is accomplished by changing the right boundary of the computational region to a wall, no slip boundary condition. The effects and setup are clearly shown by the two-dimensional distributions of the velocity vectors (Fig. 6) where the latter depicts the simulation with the confining vacuum-tank wall. A comparison of the computed performance is shown in Table 2 and implies insignificant influence from the restrictive vacuum tank.

$E(J) / m(mg)$	I (outlet)	I (tank wall)
900 / 4.2	44.3 mN-s	43.6 mN-s
1296 / 3	35.7 mN-s	35.7 mN-s
1296 / 1.5	26.5 mN-s	28.7 mN-s
1764 / 3	42.2 mN-s	43.1 mN-s

Table 2. Calculated impulse values with and without influence from the vacuum-tank wall.

The second issue that can be addressed by the code in its present state is the mass injection scheme. The thruster utilizes a gas valve and a conical nozzle to guide the cold propellant gas toward the induction coil. The duration of the pulse in the experiments was designed such that the desired amount is injected before the leading edge of the expanding gas reaches the confining cuff. A delay before discharge followed such that all the propellant is

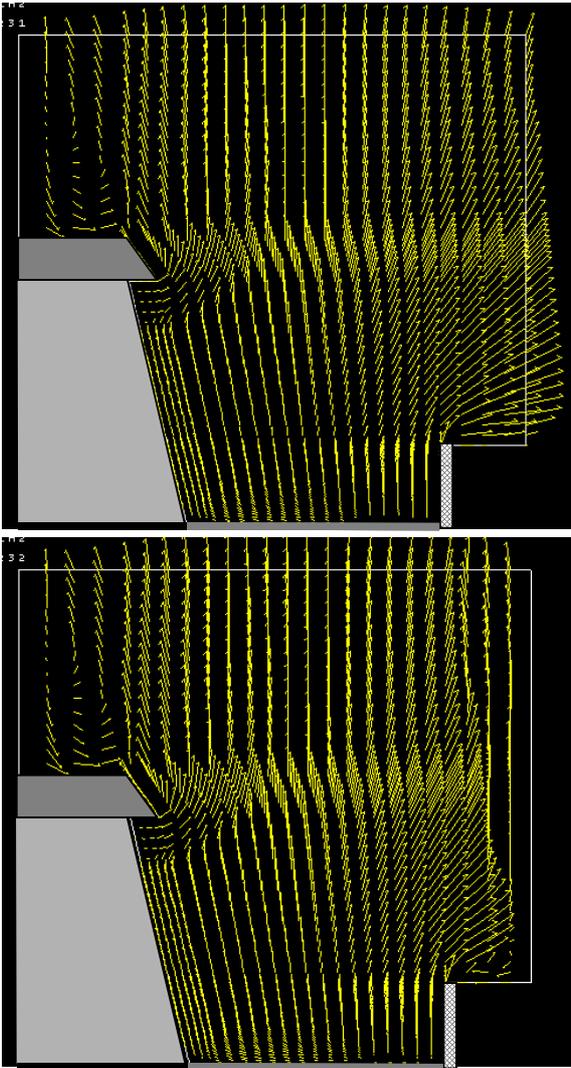


Figure 9. Velocity vector distribution depicting the influence of the wall boundary condition. Top: Outlet, Bottom: Emulation of vacuum-tank wall at the right boundary.

colder propellant's location is relatively inconsequential (whether it resides immediately downstream of the accelerating fraction or still expanding over the conical pylon) as it will be eventually swept by the fast moving portion.

The aforementioned deductions can be extrapolated as to the effect of the LRC model's plasma-inductance deficiency which resulted in underestimating the minimum current's magnitude by half. They imply that any additional acceleration due to the second current peak is minimal. If indeed the overestimation from assuming uniform initial conditions was originally equalized by the deficiency in calculating the acceleration due to second current peak then the latter's contribution is only of the order of $(26.5-23.9)\text{mN}\cdot\text{s} = 2.6\text{mN}\cdot\text{s} \sim 10\%$. This is minimal of course partly due to the lower energy levels involved in the helium experiments and thus the relative significance of the plasma's inductance. The LRC model in MACH2 needs to be amended to include the effects of plasma dynamics before higher-energy-level modeling is performed.

given the opportunity to distribute itself over the induction coil. Emulation of the process by the MACH2 code introduces the mass at the conical nozzle as helium at room temperature and subsonic speeds. This choice of the mass-flow-rate value ensured injection of the total propellant in 2 msec. (The particular simulation considered the 1.5mg case.) The two-dimensional mass density distributions depicted in Figures 7 and 8 outline the evolution and behavior of the cold propellant as it expands toward the induction coil. At 2msec the flow rate is interrupted and the emulated discharge is initiated which is somewhat dissimilar from the experimental setup that enforced a delay such that the mass is distributed as uniformly as possible. In other words, the MACH2 simulation will address non-uniformities from the mass-injection scheme that are much more profound than during actual operation. One of the main differences is that the MACH2 scheme prevents a significant portion of the mass to interact with the fast-rising magnetic field, (the propellant still flowing along the pylon in Figure 8, 2msec).

Comparisons of the calculated impulse values between the uniformly distributed properties and this injection scheme for $V_0 = 12\text{kV}$ and $m = 1.5\text{mg}$ show insignificant influence of the latter. Specifically, uniform initial conditions predict an impulse of 26.5 mN-s while the more pragmatic mass-injection scheme calculates 23.9 mN-s. The discrepancy is insignificant, especially considering that during the experiments the mass was given the opportunity to distribute itself as uniformly as possible before the voltage drop was applied. A plausible explanation arises from interrogation of the axial distributions of the magnetic field temperature and ionization level, but can as well be deduced by noting that only a portion of the propellant (of the order of the diffusion depth) adjacent to the coil participates in the magnetic flux coupling and current induction. This hotter, ionized fraction is subject to electromagnetic acceleration, but as it propels downstream it entrains the remainder colder propellant. This

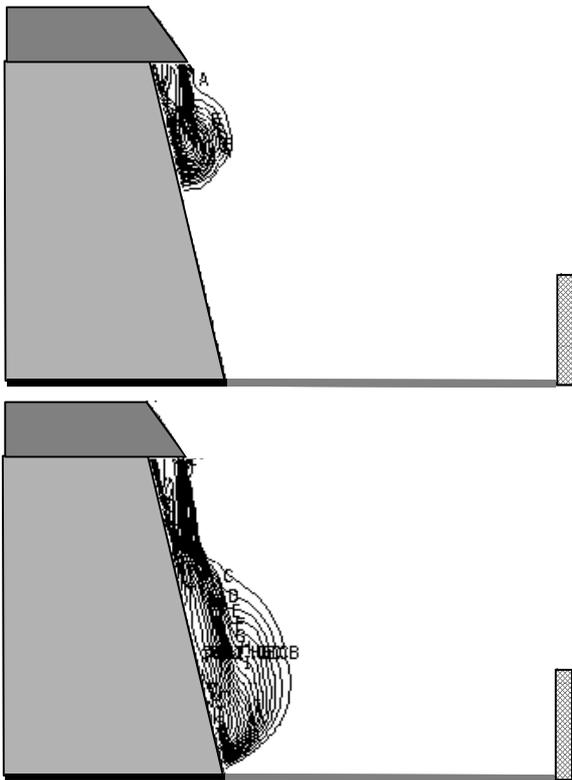


Figure 10. Mass-density evolution as it is injected from the conical nozzle, (0.3 msec and 0.8msec).

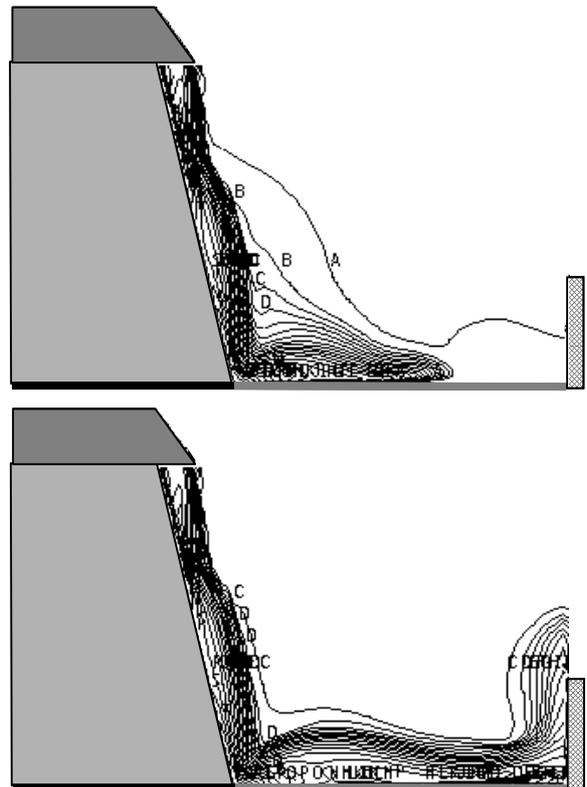


Figure 11. Mass-density evolution as it is injected from the conical nozzle, (1.2msec and 2msec). At 2msec the emulated discharge is initiated.

CONCLUSIONS

The magnetohydrodynamics code, MACH2 was employed to model the performance of the Pulsed Inductive Thruster (PIT) operated with helium and argon propellants within a range of 900J-1764J and propellant mass range of 0.75mg-9.2mg. Comparisons between predicted and experimentally measured impulse values demonstrated excellent agreement. The effects of a restrictive vacuum tank used to obtain the experimental data were examined by simulating a wall, no-slip boundary condition at the location of the vacuum tank. Performance was insignificantly affected. Effects of the mass injection-scheme were also investigated for one energy and mass case to also show that performance was minimally affected by the non-uniform distribution of the injected propellant over the induction coil.

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